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Seventh Semester B.E. Degree Examination, Feb./Mar.2022 Numerical Methods and Applications

Time: 3 hrs.

Max. Marks: 100

**Note: 1. Answer any FIVE full questions, choosing ONE full question from each module.
2. Missing data may be suitably assumed.**

Module-1

- 1 a. Find the real root of the equation, $\cos x = 3x - 1$ correct to three decimal places using iteration method. (10 Marks)
- b. Solve the system of linear equations by using Gauss elimination method,
 $4x_1 + 2x_2 + 3x_3 = 4$
 $2x_1 + 2x_2 + x_3 = 6$
 $x_1 - x_2 + x_3 = 0$ (10 Marks)

OR

- 2 a. Using Newton-Raphson method, find the real root of $x \log_{10} x = 1.2$ correct to five decimal places. (10 Marks)
- b. Solve the following set of linear equations by Gauss-Seidel method.
 $10x_1 + x_2 + x_3 = 12$
 $2x_1 + 10x_2 + x_3 = 13$
 $2x_1 + 2x_2 + 10x_3 = 14$
 Carryout five iterations. (10 Marks)

Module-2

- 3 a. Using Lagrange's interpolation formula, find a polynomial which passes through the points (0, -12), (1, 0), (3, 6), (4, 12). (05 Marks)
- b. Using Lagrange's interpolation formula, find the value of 'y' corresponding to $x = 10$ from the following table: (05 Marks)

| | | | | |
|----------|-----|----|----|----|
| x | 5 | 6 | 9 | 11 |
| y = f(x) | -12 | 13 | 14 | 16 |

- c. The values of $\sin x$ are given below for different values of x . Find the value of $\sin 32^\circ$ using Newton's forward interpolation formula. (10 Marks)

| | | | | | |
|-----------|------------|------------|------------|------------|------------|
| x = | 30° | 35° | 40° | 45° | 50° |
| y = sin x | 0.5 | 0.5736 | 0.6428 | 0.7071 | 0.7660 |

OR

- 4 a. Use Newton's divided difference formula and evaluate $f(6)$ given,

| | | | | | |
|------|-----|-----|------|------|------|
| x | 5 | 7 | 11 | 13 | 21 |
| f(x) | 150 | 392 | 1452 | 2366 | 9702 |

(10 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
2. Any revealing of identification, appeal to evaluator and /or equations written eg. 42+8 = 50, will be treated as malpractice.

- b. The following data gives the melting point of an alloy of lead and zinc, where t is the temperature in degrees C and P is the percentage of lead in the alloy. Find the melting point of the alloy containing 84% lead. Use Newton's backward difference formula.

| | | | | | | |
|---|-----|-----|-----|-----|-----|-----|
| P | 40 | 50 | 60 | 70 | 80 | 90 |
| t | 184 | 204 | 226 | 250 | 276 | 304 |

(10 Marks)

Module-3

- 5 a. Find the value of $\int_0^1 \frac{dx}{1+x^2}$, taking 5 sub intervals by trapezoidal rule. Correct to five significant figures. Also compare it with its exact value. (10 Marks)
- b. Evaluate $\int_2^3 \frac{\cos 2x}{1+\sin x}$ by using Gauss quadrature three point formula. (10 Marks)

OR

- 6 a. The velocity of a train which starts from rest is given by the following table Table Q6 (a). Estimate approximately the total distance run in 20 minutes using Simpson's $\frac{1}{3}$ rule. (10 Marks)

| | | | | | | | | | | |
|----------|----|------|----|------|------|----|------|----|-----|----|
| t(min) | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 | 20 |
| v(km/hr) | 16 | 28.8 | 40 | 46.4 | 51.2 | 32 | 17.6 | 8 | 3.2 | 0 |

Table O6 (a)

- b. Evaluate the integral $I = \int_0^{0.2} \int_0^{0.2} e^y \sin x \, dx \, dy$ by ,
- (i) Trapezoidal rule with $h = k = 0.2$ and
- (ii) Simpson's $\frac{1}{3}$ rule with $h = k = 0.1$ (10 Marks)

Module-4

- 7 a. Find by Taylor's series method, the values of y at $x = 0.1$ and $x = 0.2$ to five places of decimals from $\frac{dy}{dx} = x^2y - 1$, $y(0) = 1$. (10 Marks)
- b. Given $\frac{dy}{dx} = \frac{1}{2}(1+x^2)y^2$ and $y(0) = 1$, $y(0.1) = 1.06$, $y(0.2) = 1.12$, $y(0.3) = 1.21$. Evaluate $y(0.4)$ by Milne's predictor corrector method. (10 Marks)

OR

- 8 a. Solve by Euler's method the following differential equation at $x = 0.1$, correct to four decimal places, with the initial condition $y(0) = 1$, $h = 0.02$, $\frac{dy}{dx} = \frac{y-x}{y+x}$. (10 Marks)
- b. Using Runge-Kutta method of order 4, find 'y' for $x = 0.1, 0.2$ given that $\frac{dy}{dx} = xy + y^2$, $y(0) = 1$. (10 Marks)



**Module-5**

- 9 The deflection of a beam is governed by the equation $\frac{d^4y}{dx^4} + 81y = \phi(x)$, where $\phi(x)$ is given by the table,

| | | | |
|-----------|---------------|---------------|-----|
| x | $\frac{1}{3}$ | $\frac{2}{3}$ | 1 |
| $\phi(x)$ | 81 | 162 | 243 |

and boundary condition $y(0) = y'(0) = y''(1) = y'''(1) = 0$. Evaluate the deflection at the pivoted points of the beam using three sub-intervals. (20 Marks)

OR

- 10 a. Solve the equation $\frac{\partial u}{\partial y} = \frac{\partial^2 u}{\partial x^2}$ subject to the conditions $u(x,0) = \sin \pi x$, $0 \leq x \leq 1$; $u(0,t) = 0$, $u(1,t) = 0$, using Crank-Nicolson method. Carryout computations for two levels, taking $h = \frac{1}{3}$, $K = \frac{1}{36}$. (10 Marks)
- b. Find the solution of the initial boundary value problem, $\frac{\partial^2 u}{\partial t^2} = \frac{\partial^2 u}{\partial x^2}$, $0 \leq x \leq 1$; subject to the initial conditions $u(x,0) = \sin \pi x$, $0 \leq x \leq 1$, $\left(\frac{\partial u}{\partial x}\right)(x,0) = 0$, $0 \leq x \leq 1$ and the boundary conditions $u(0,t) = 0$, $u(1,t) = 0$, $t > 0$, by using in the explicit scheme. Take $h = K = 0.2$. (10 Marks)

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